We will discuss relationships between hypergeometric functions (ordinary and over finite fields) and Fourier coefficients of modular forms. Among them are the supercongruence conjectures of Rodriguez-Villegas. We will outline recent work on proving one of these conjectures using a function which extends Greenes hypergeometric function over finite fields to the p-adic setting.